Deep Learning Intuition

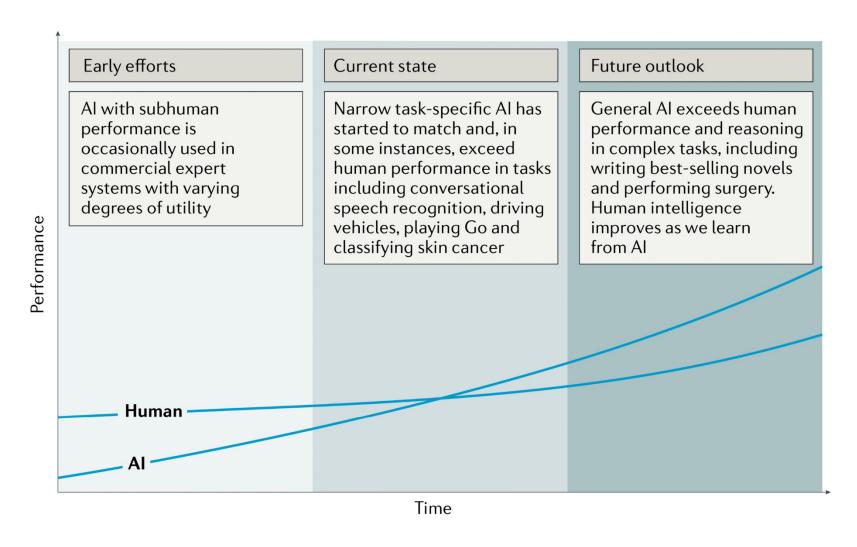






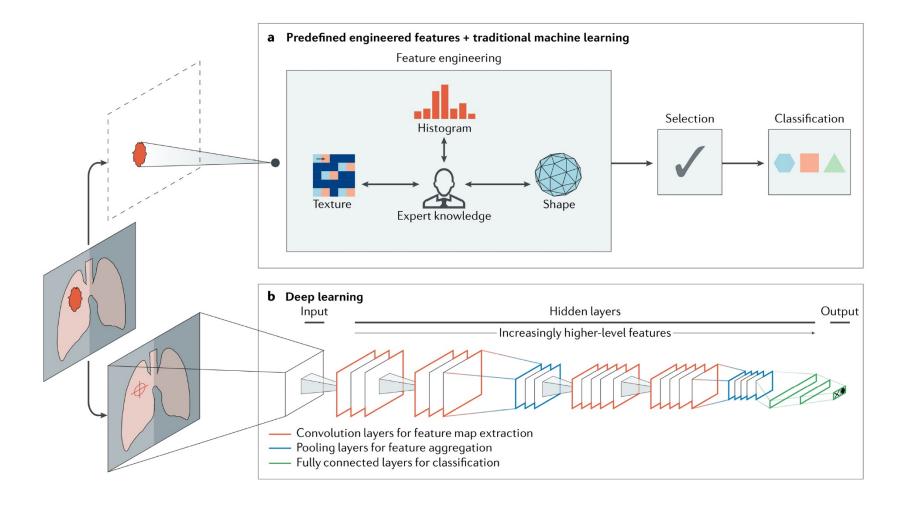
Ahmed Hosny

Deep Learning



Ahmed Hosny, Chintan Parmar, John Quackenbush, Lawrence H Schwartz and Hugo JWL Aerts

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What is the intuition behind neural networks?

How do neural networks learn?

How to train neural networks?

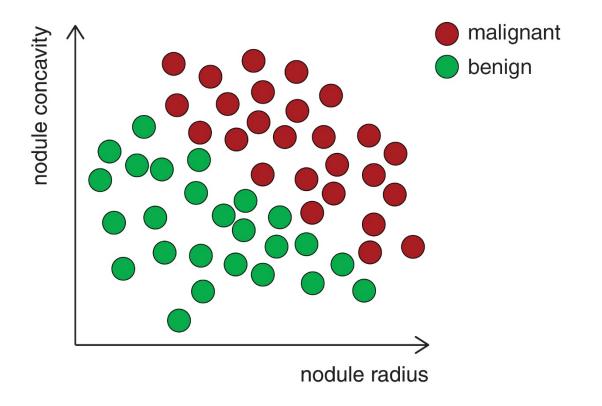
What is the intuition behind neural networks?

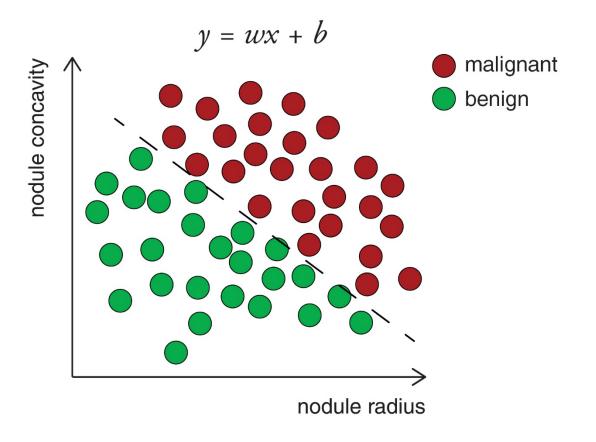
How do neural networks learn?

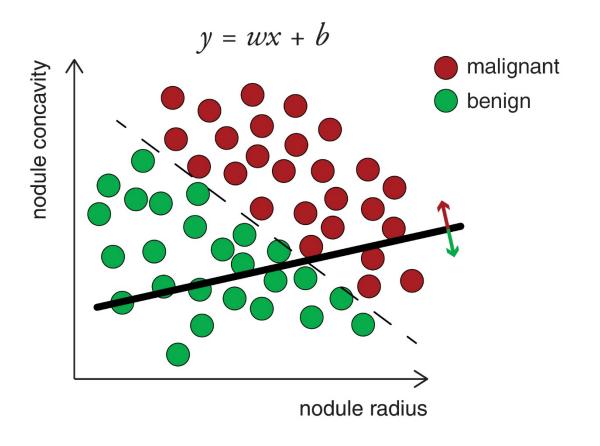
How to train neural networks?

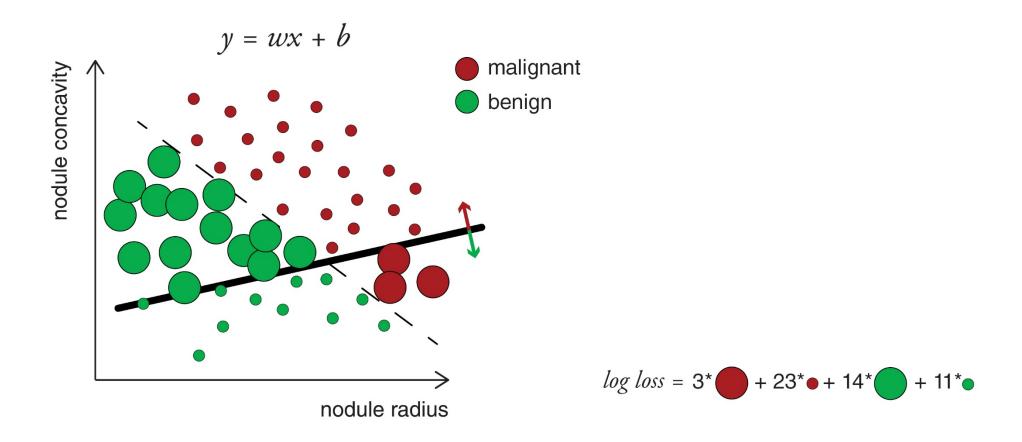
Machine Learning: 4 Main Components

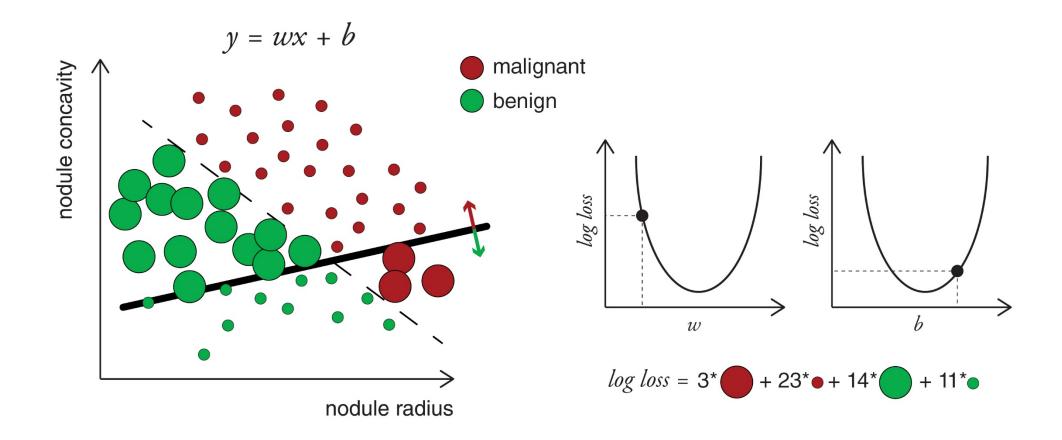
- Data
- Model/Representation
- Cost/Error/Loss of model
- Model Optimizer

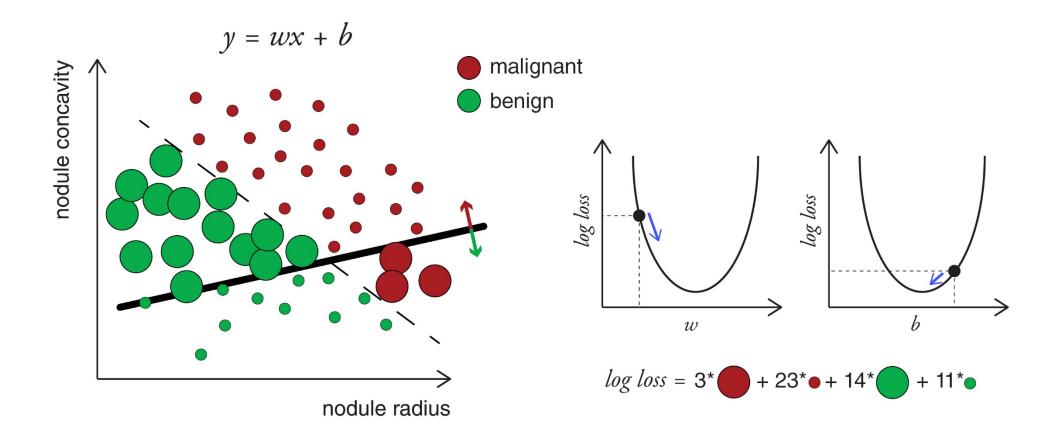


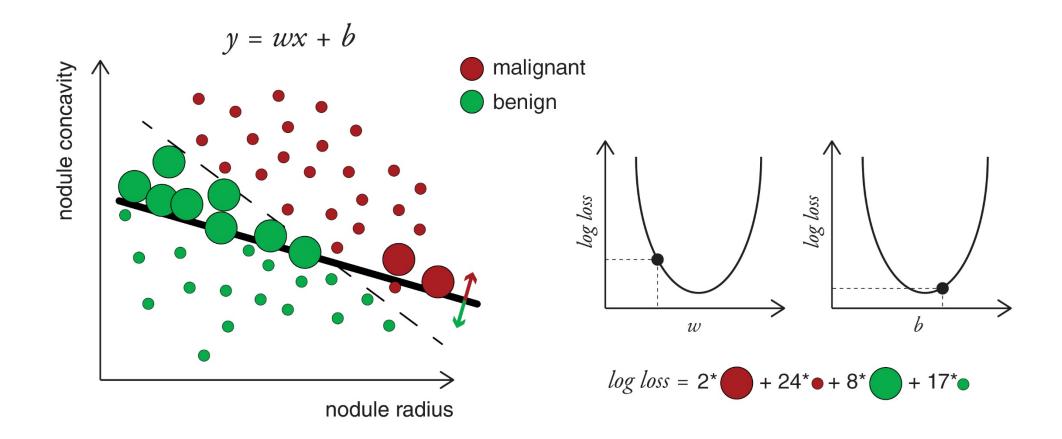


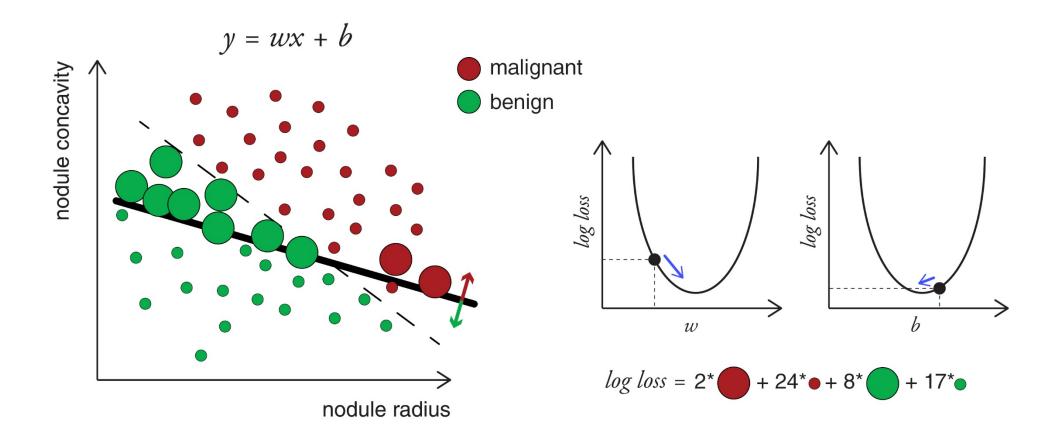


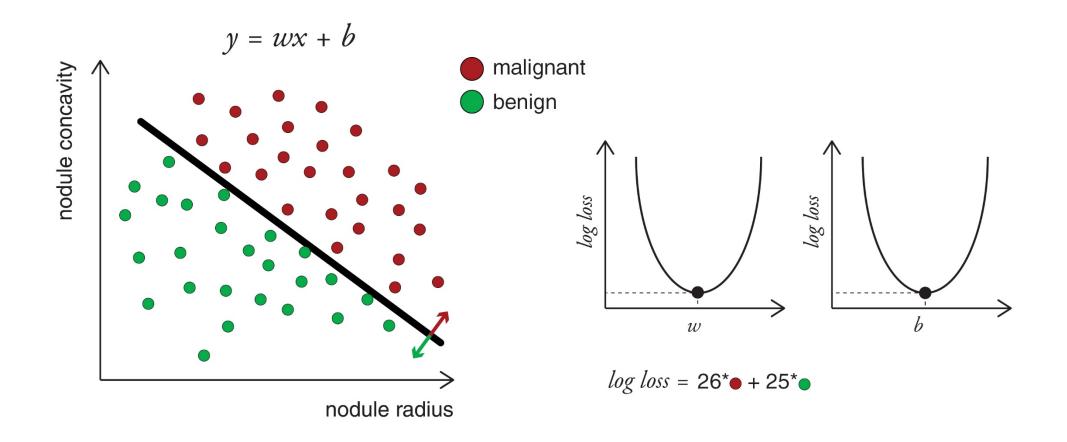


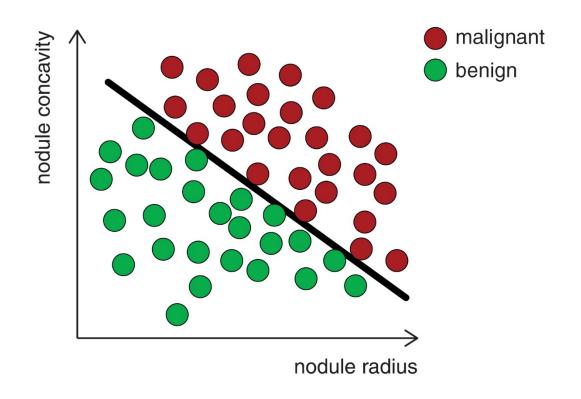


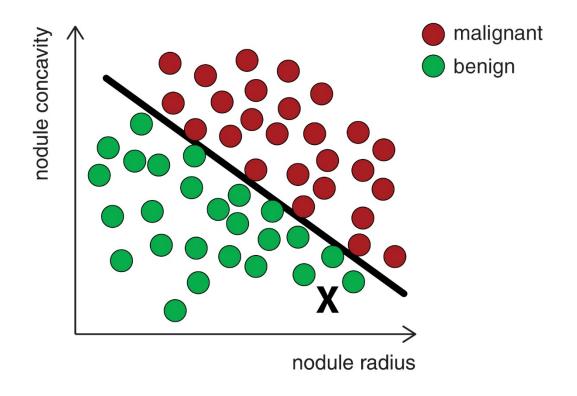


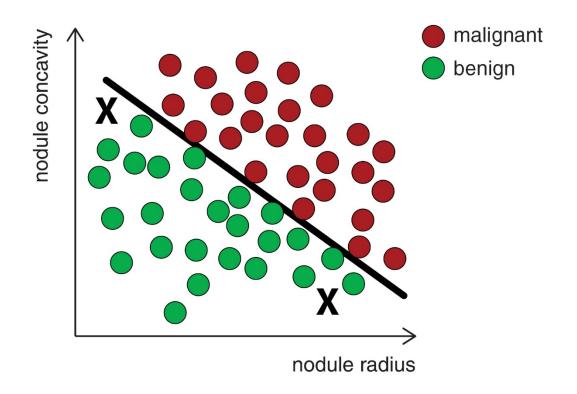


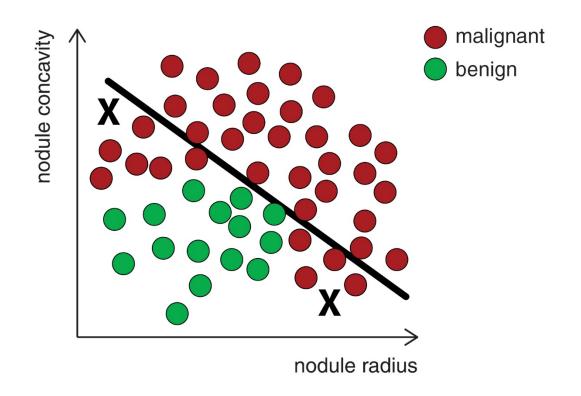


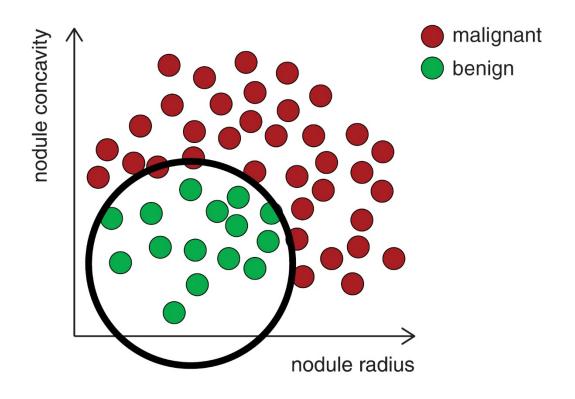


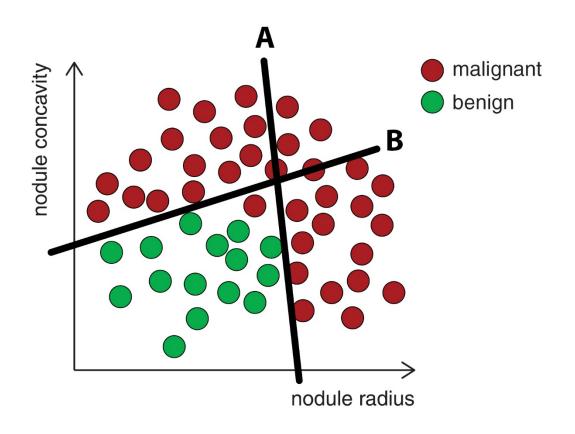


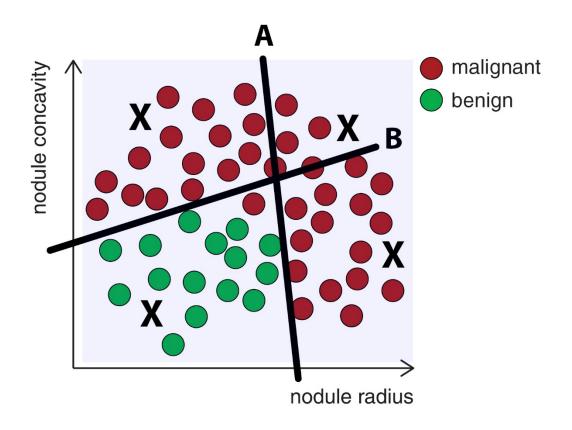


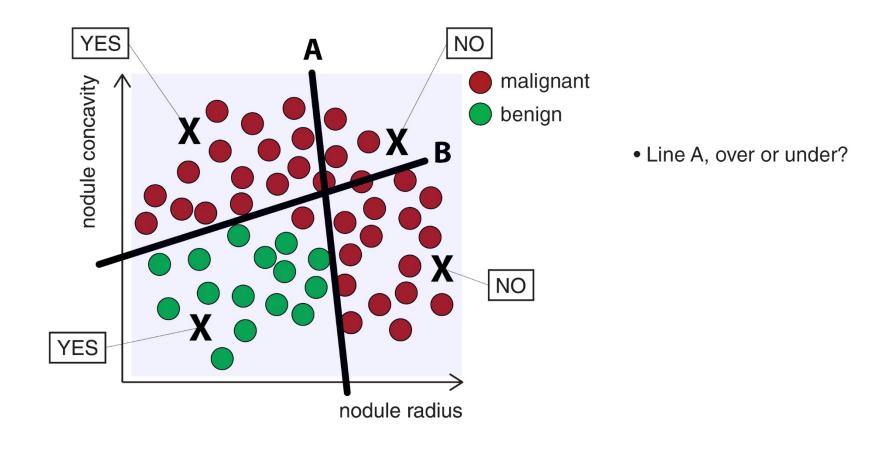


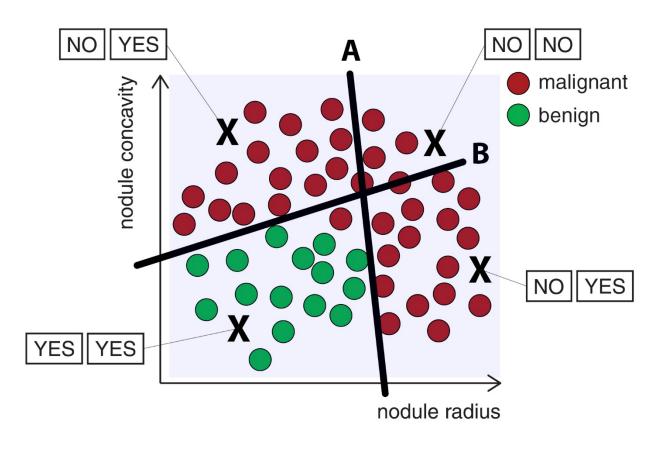




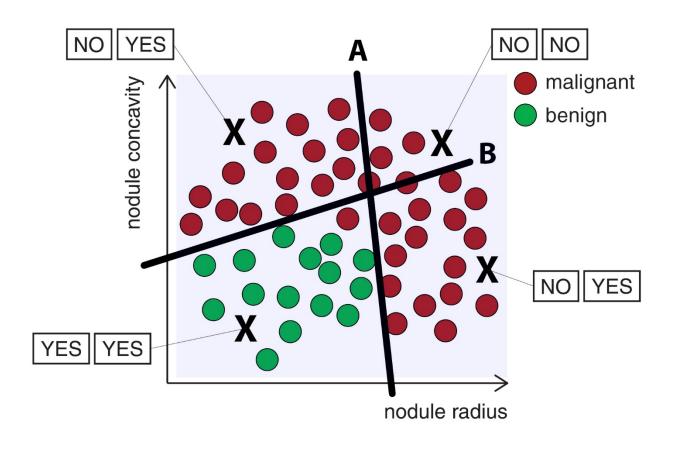




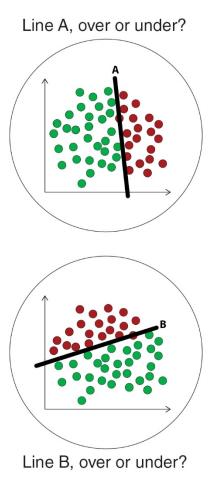


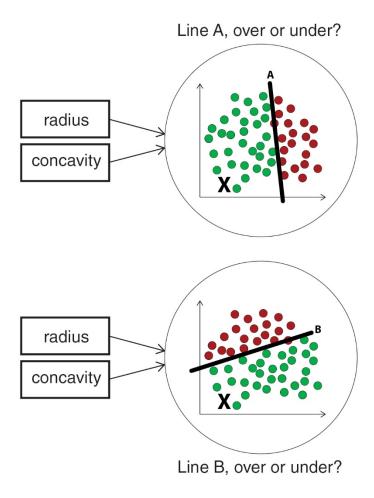


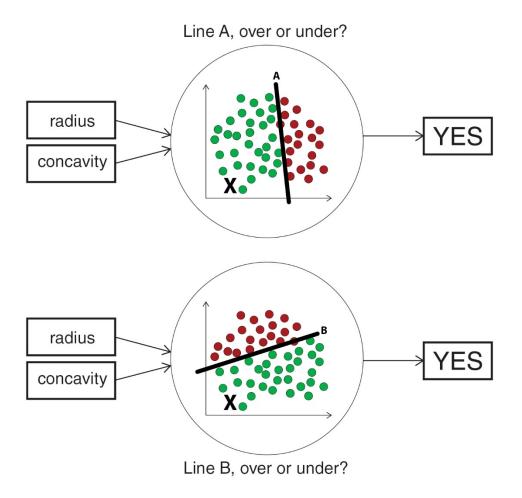
- Line A, over or under?
- Line B, over or under?

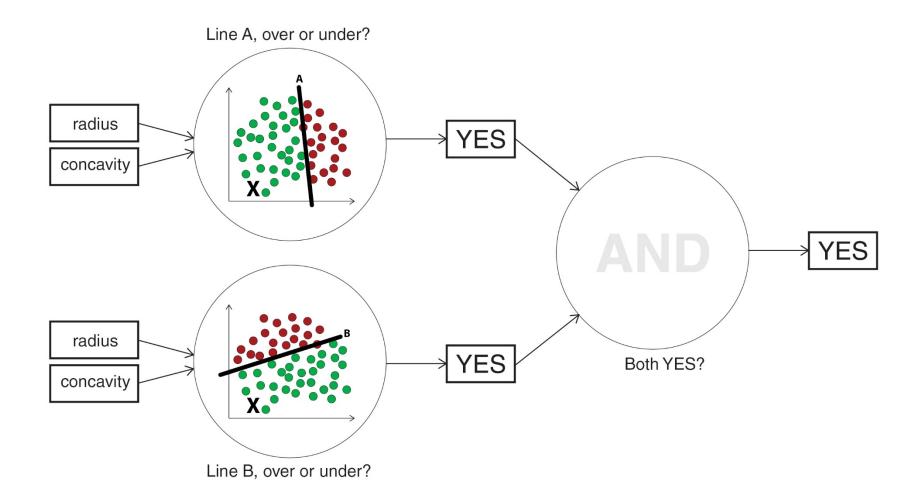


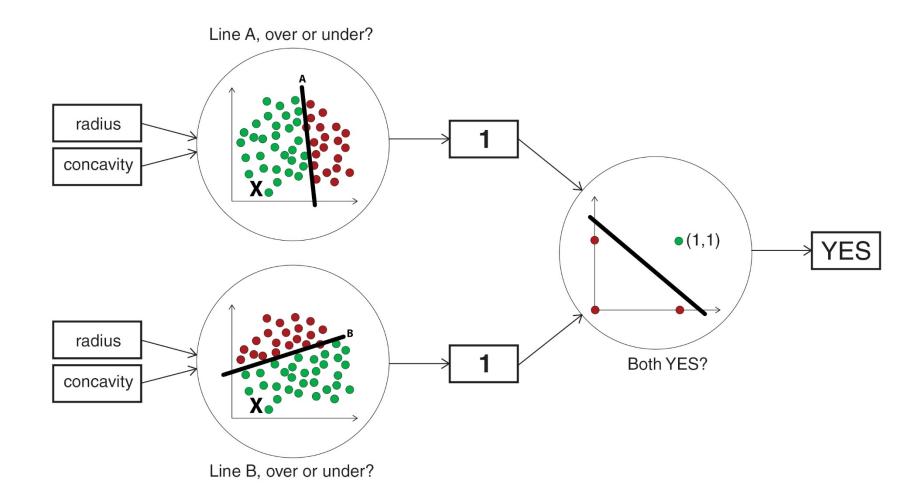
- Line A, over or under?
- Line B, over or under?
- Both YES?



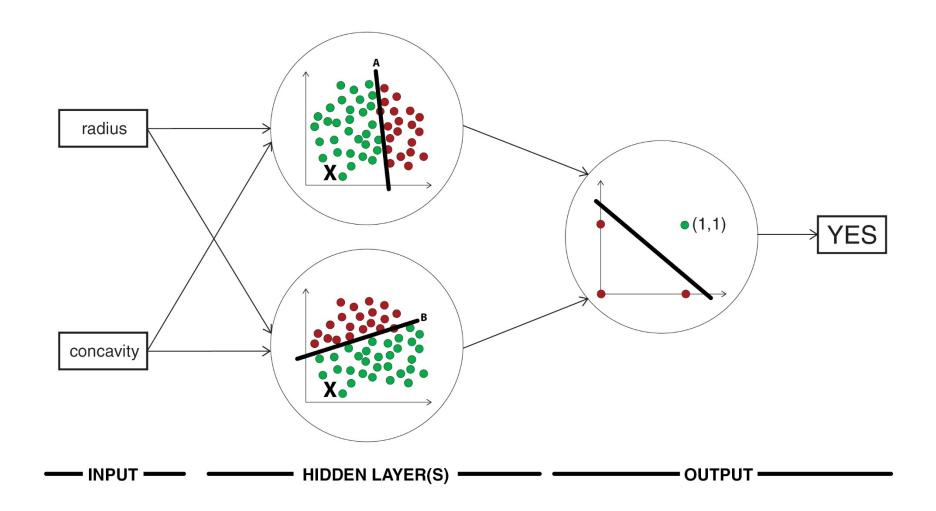




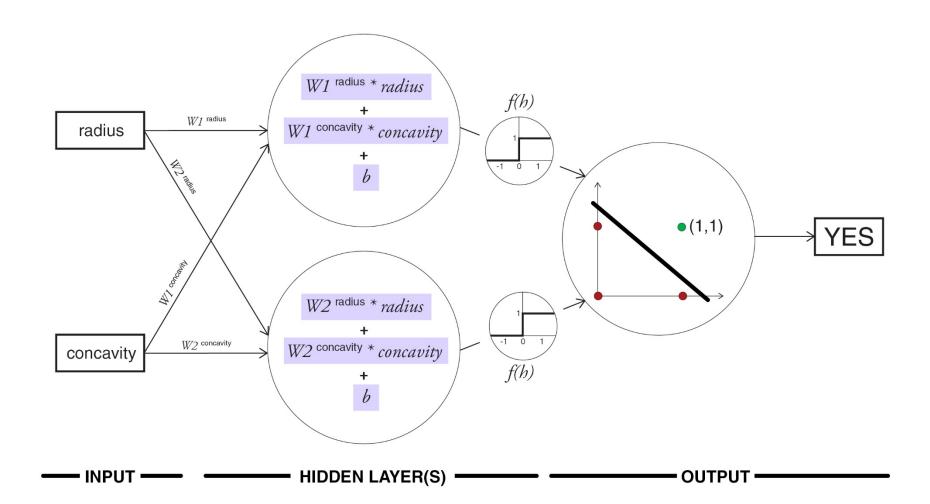


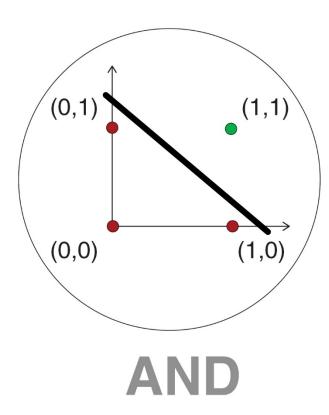


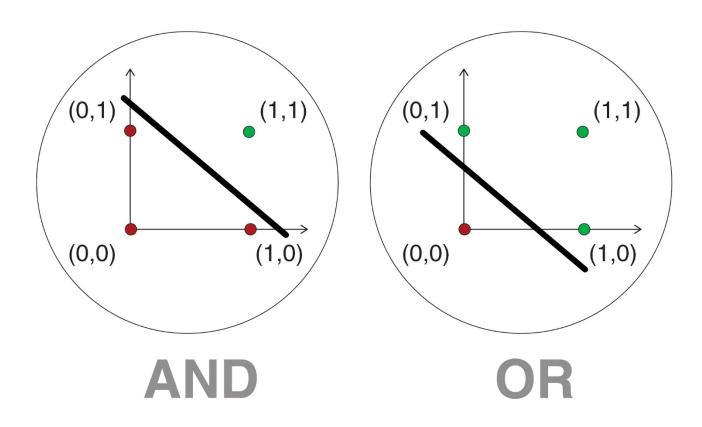
A Neural Network

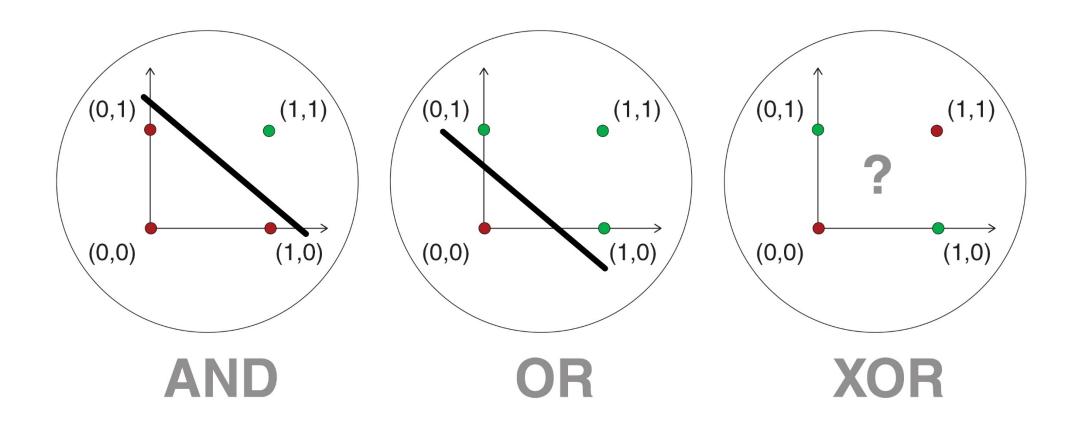


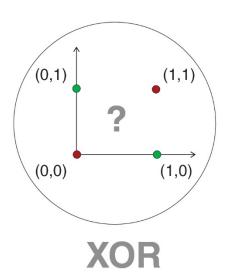
A Neural Network

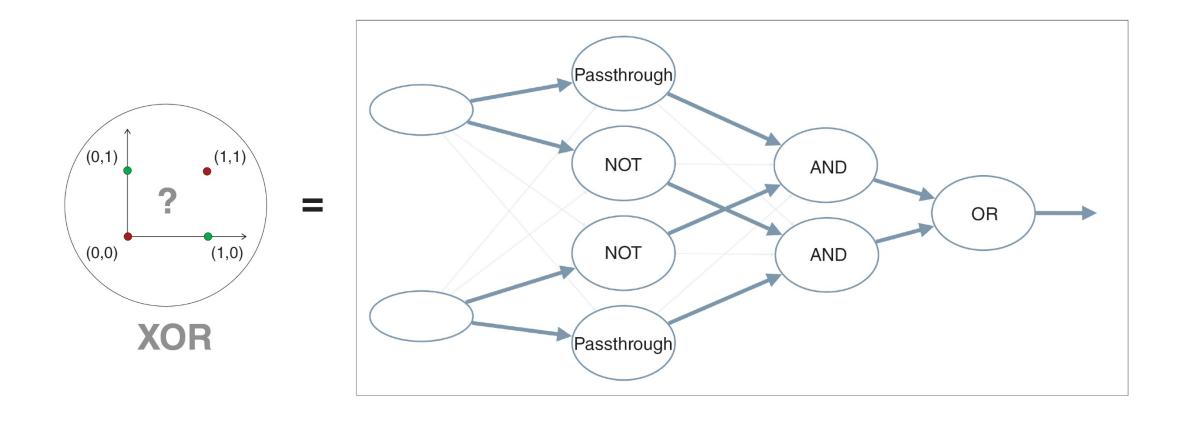


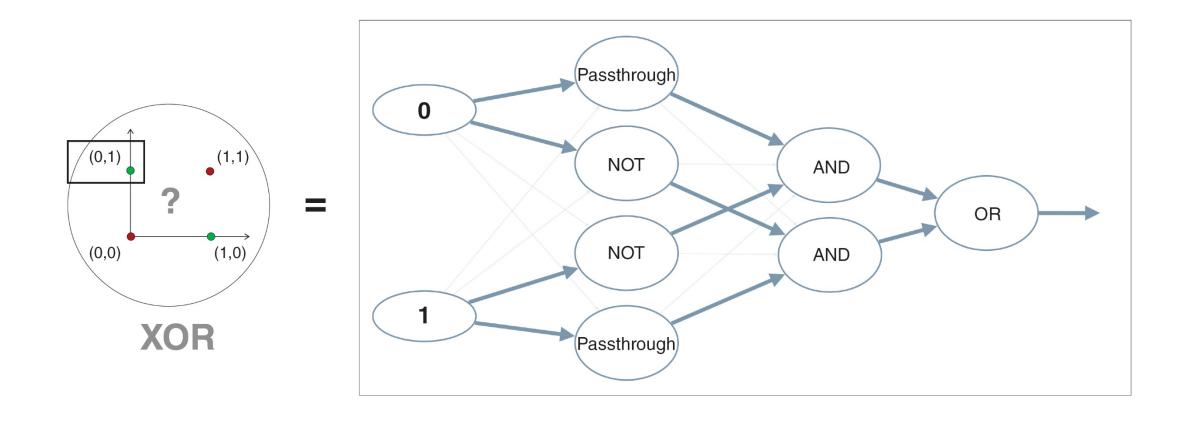


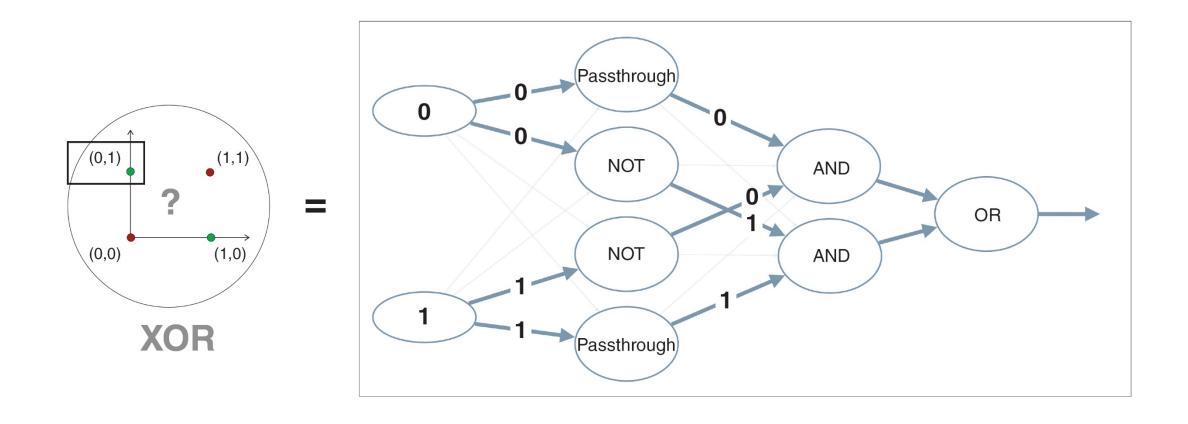


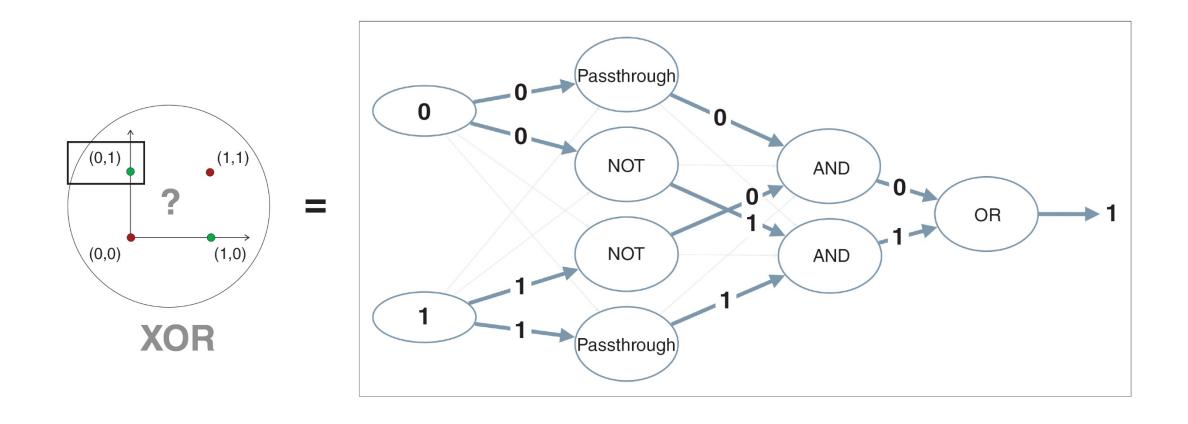












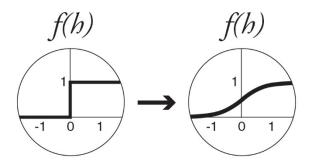
What is the intuition behind neural networks?

How do neural networks learn?

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Backpropagation & Gradient Descent in Neural Networks

NATURE VOL. 323 9 OCTOBER 1986 -LETTERS TO NATURE



Learning representations by back-propagating errors

David E. Rumelhart*, Geoffrey E. Hinton† & Ronald J. Williams*

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We describe a new learning procedure, back-propagation, for networks of neurone-like units. The procedure repeatedly adjusts the weights of the connections in the network so as to minimize a measure of the difference between the actual output vector of the net and the desired output vector. As a result of the weight adjustments, internal 'hidden' units which are not part of the input or output come to represent important features of the task domain. and the regularities in the task are captured by the interactions of these units. The ability to create useful new features distinguishes back-propagation from earlier, simpler methods such as

the perceptron-convergence procedure1. There have been many attempts to design self-organizing neural networks. The aim is to find a powerful synaptic modification rule that will allow an arbitrarily connected neural network to develop an internal structure that is appropriate for a particular task domain. The task is specified by giving the desired state vector of the output units for each state vector of the input units. If the input units are directly connected to the output units it is relatively easy to find learning rules that iteratively adjust the relative strengths of the connections so as to progressively reduce the difference between the actual and desired output vectors2. Learning becomes more interesting but

more difficult when we introduce hidden units whose actual or desired states are not specified by the task. (In perceptrons, there are 'feature analysers' between the input and output that are not true hidden units because their input connections are fixed by hand, so their states are completely determined by the input vector: they do not learn representations.) The learning procedure must decide under what circumstances the hidden units should be active in order to help achieve the desired input-output behaviour. This amounts to deciding what these units should represent. We demonstrate that a general purpose and relatively simple procedure is powerful enough to construct appropriate internal representations

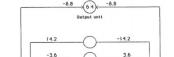
The simplest form of the learning procedure is for layered networks which have a layer of input units at the bottom; any number of intermediate layers; and a layer of output units at the top. Connections within a layer or from higher to lower layers are forbidden, but connections can skip intermediate ayers. An input vector is presented to the network by setting the states of the input units. Then the states of the units in each layer are determined by applying equations (1) and (2) to the connections coming from lower layers. All units within a layer have their states set in parallel, but different layers have their states set sequentially, starting at the bottom and working upwards until the states of the output units are determined

The total input, x_j , to unit j is a linear function of the outputs, y_i , of the units that are connected to j and of the weights, w_{ji} ,

Units can be given biases by introducing an extra input to each unit which always has a value of 1. The weight on this extra input is called the bias and is equivalent to a threshold of the opposite sign. It can be treated just like the other weights.

A unit has a real-valued output, y, which is a non-linear function of its total input

$$y_j = \frac{1}{1 + e^{-x_j}}$$
 (2)



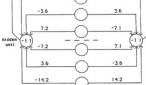


Fig. 1 A network that has learned to detect mirror symmetry in the input vector. The numbers on the arcs are weights and the numbers inside the nodes are biases. The learning required 1,425 sweeps through the set of 64 possible input vectors, with the weights being adjusted on the basis of the accumulated gradient after eac sweep. The values of the parameters in equation (9) were $\varepsilon = 0.1$ and $\alpha = 0.9$. The initial weights were random and were unif distributed between -0.3 and 0.3. The key property of this solution is that for a given hidden unit, weights that are symmetric about the middle of the input vector are equal in magnitude and opposite in sign. So if a symmetrical pattern is presented, both hidden units will receive a net input of 0 from the input units, and, because the hidden units have a negative bias, both will be off. In this case the output unit, having a positive bias, will be on. Note that the weights on each side of the midpoint are in the ratio 1:2:4. This ensures that each of the eight patterns that can occur above the midpoint sends a unique activation sum to each hidden unit, so the only pattern below the midpoint that can exactly balance this sum is the symmetrical one. For all non-symmetrical patterns, both hidden units will receive non-zero activations from the input units. The two hidden units have identical patterns of weights but with opposite signs, so for every non-symmetric pattern one hidden unit will come on and suppress the output unit.

It is not necessary to use exactly the functions given in equations (1) and (2). Any input-output function which has a bounded derivative will do. However, the use of a linear function for combining the inputs to a unit before applying the nonlinearity greatly simplifies the learning procedure.

The aim is to find a set of weights that ensure that for each input vector the output vector produced by the network is the same as (or sufficiently close to) the desired output vector. If there is a fixed, finite set of input-output cases, the total error in the performance of the network with a particular set of weights can be computed by comparing the actual and desired output vectors for every case. The total error, E, is defined as

 $E = \frac{1}{2} \sum_{i} (y_{j,c} - d_{j,c})^2$

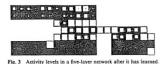
where c is an index over cases (input-output pairs), j is an index over output units, y is the actual state of an output unit and d is its desired state. To minimize E by gradient descent it is necessary to compute the partial derivative-of-E-with respect to each weight in the network. This is simply the sum of the partial derivatives for each of the input-output cases. For a given case, the partial derivatives of the error with respect to each weight are computed in two passes. We have already described the forward pass in which the units in each layer have their states determined by the input they receive from units in lower layers using equations (1) and (2). The backward pass which propagates derivatives from the top layer back to the bottom one is more complicated



LETTERSTONATURE



Fig. 2 Two isomorphic family trees. The information can be expressed as a set of triples of the form (person 1)(relationship) (person 2), where the possible relationships are {father, mother, husband, wife, son, daughter, uncle, aunt, brother, sister, nephew, niece) A layered net can be said to 'know' these triples if it can produce the third term of each triple when given the first two. The first two terms are encoded by activating two of the input units. and the network must then complete the proposition by activating the output unit that represents the third term



The bottom layer has 24 input units on the left for representing (person 1) and 12 input units on the right for representing the relationship. The white squares inside these two groups show the activity levels of the units. There is one active unit in the first group representing Colin and one in the second group representing the relationship 'has-aunt'. Each of the two input groups is totally connected to its own group of 6 units in the second layer. These groups learn to encode people and relationships as distributed patterns of activity. The second layer is totally connected to the central layer of 12 units, and these are connected to the penultimate layer of 6 units. The activity in the penultimate layer must activate the correct output units, each of which stands for a particula nerson 2) In this case, there are two correct answers (marked by black dots) because Colin has two aunts Both the input units and the output units are laid out spatially with the English people in one row and the isomorphic Italians immediately b

The backward pass starts by computing $\partial E/\partial y$ for each of the output units. Differentiating equation (3) for a particular case, c, and suppressing the index c gives

$$\partial E/\partial y_i = y_i - d_i$$
 (4)

We can then apply the chain rule to compute $\partial E/\partial x_j$

$$\partial E/\partial x_j = \partial E/\partial y_j \cdot dy_j/dx_j$$

Differentiating equation (2) to get the value of dy_i/dx_j and

$$\partial E/\partial x_i = \partial E/\partial y_i \cdot y_i (1-y_i)$$
 (5)

This means that we know how a change in the total input x to an output unit will affect the error. But this total input is just a linear function of the states of the lower level units and it is also a linear function of the weights on the connections, so it is easy to compute how the error will be affected by changing these states and weights. For a weight w_{ji} , from i to j the

$$\partial E/\partial w_{ji} = \partial E/\partial x_j \cdot \partial x_j/\partial w_{ji}$$

= $\partial E/\partial x_j \cdot y_i$ (6)

and for the output of the ith unit the contribution to aE/ay,

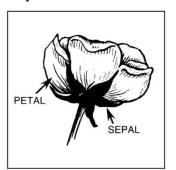
† To whom correspondence should be addressed

David E. Rumelhart, Geoffrey E. Hinton & Ronald J. Williams

Learning Representations by Back-propagating Errors Nature - 1986

Iris Dataset

Inputs



petal length & width sepal length & width

Outputs



Iris Versicolor



Iris Setosa



Iris Virginica

✓ Data: iris dataset label features petal length petal width (sepal length sepal width

✓ Data: iris dataset

✓ Model: 3-layer neural network

sigmoid

$$S(x)=rac{1}{1+e^{-x}}$$

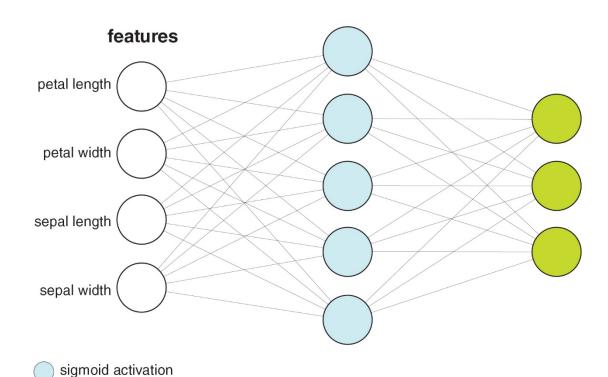
softmax

$$\sigma(\mathbf{z})_j = rac{e^{z_j}}{\sum_{k=1}^K e^{z_k}}$$
 for j = 1, ..., K .

label



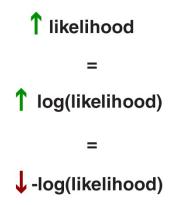
softmax activation

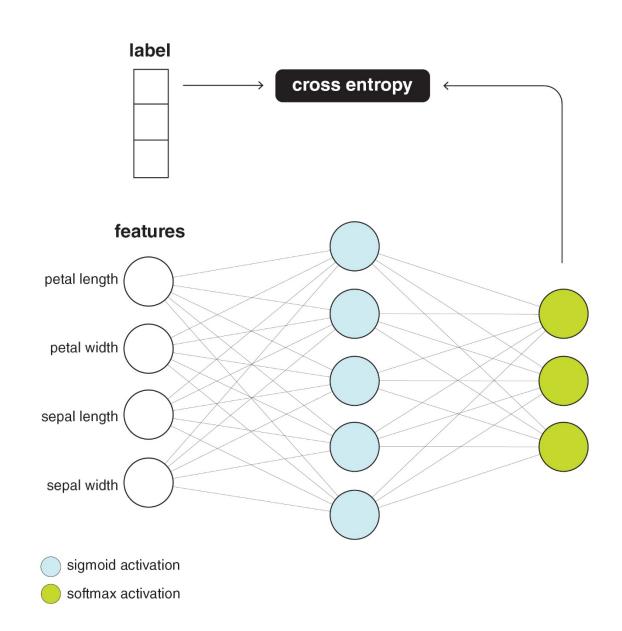


✓ Data: iris dataset

✓ Model: 3-layer neural network

✓ Loss: cross entropy



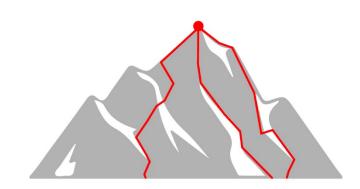


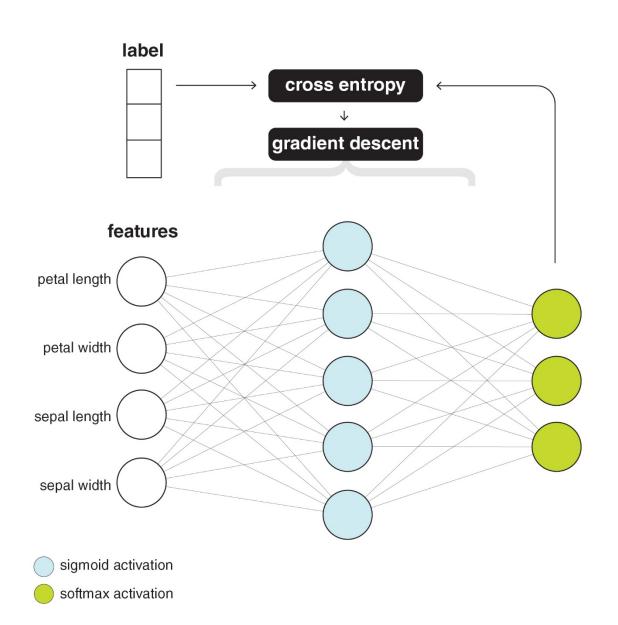
✓ Data: iris dataset

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✓ Loss: cross entropy

✓ Optimizer: gradient descent





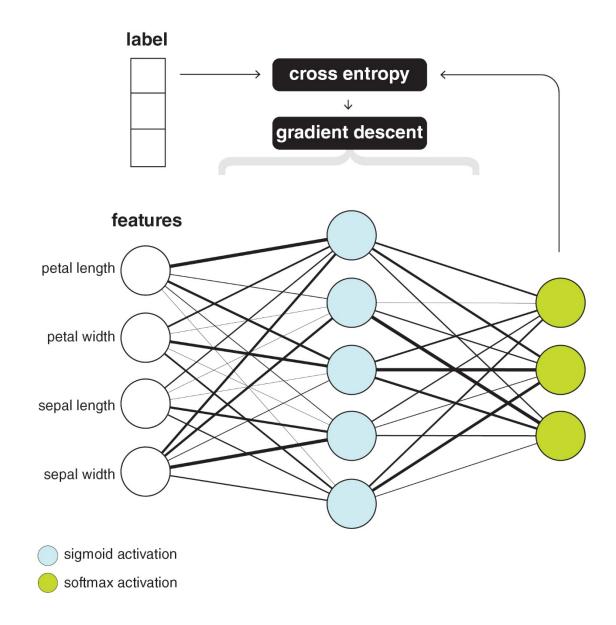
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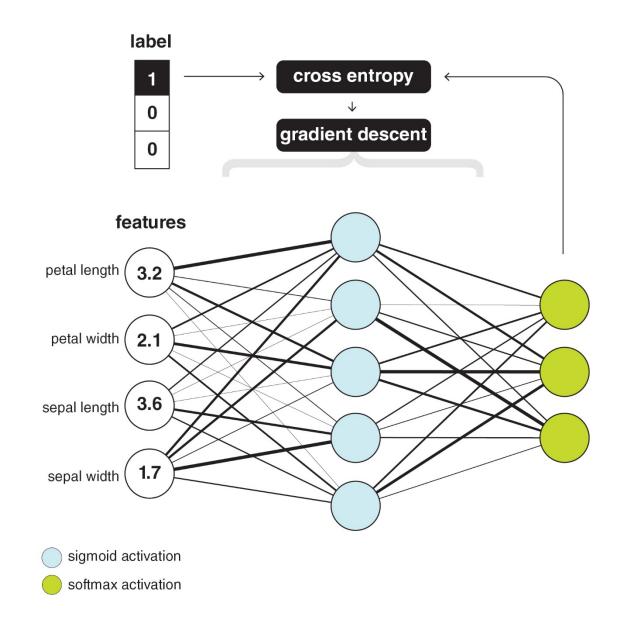
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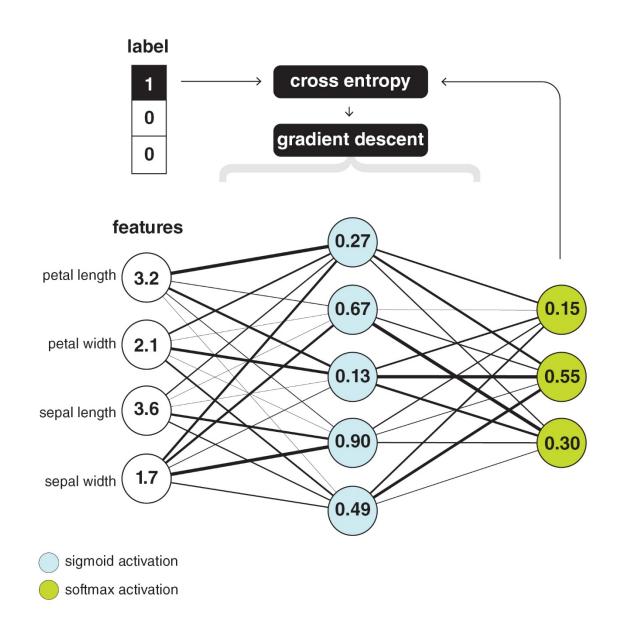
1. parameter initialization



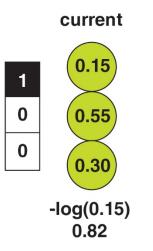
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- ✓ **Model:** 3-layer neural network
- ✓ Loss: cross entropy
- ✓ Optimizer: gradient descent
- 1. parameter initialization
- 2. data input

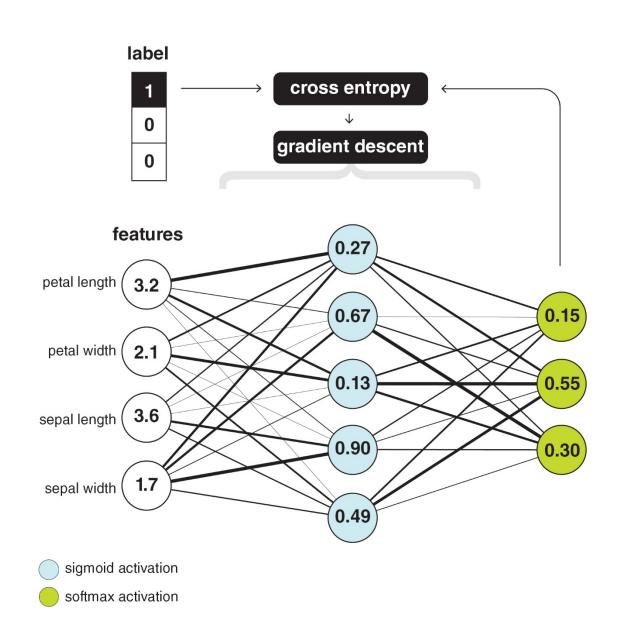


- ✓ Data: iris dataset
- ✓ **Model:** 3-layer neural network
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- ✓ Optimizer: gradient descent
- 1. parameter initialization
- 2. data input
- **3.** forward propagation

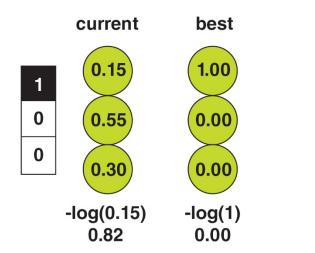


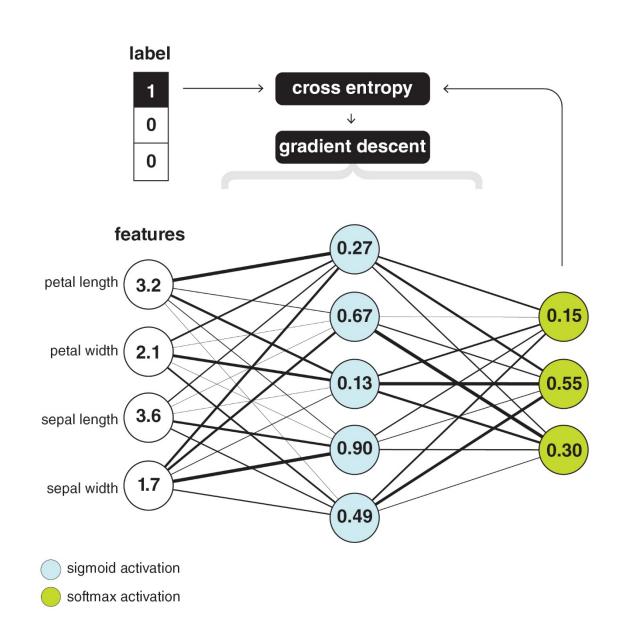
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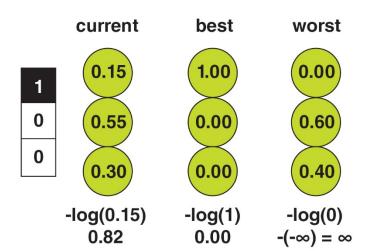


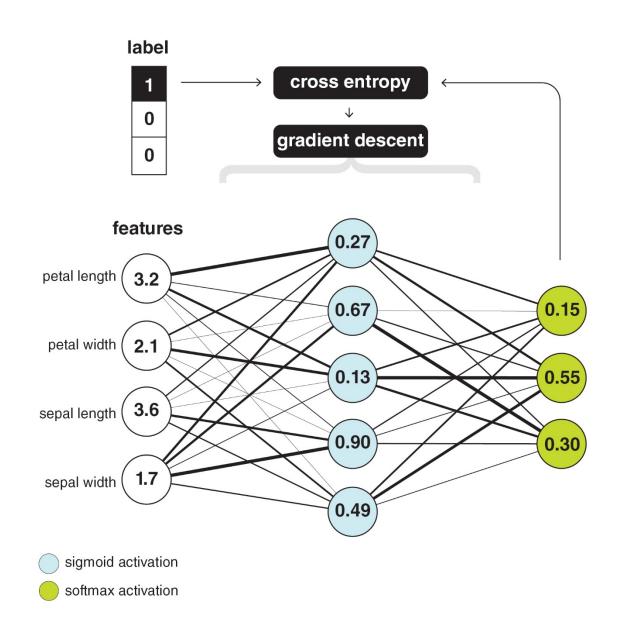
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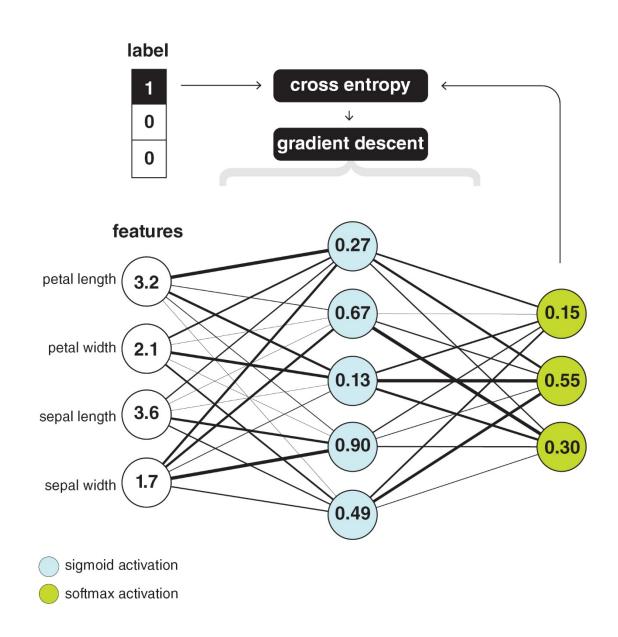


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- 4. loss calculation
- **5.** backpropagation + updates

 $\Delta w \propto$ - gradient

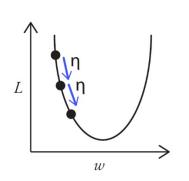
$$= - \frac{\partial \mathbf{W}}{\partial \mathbf{L}}$$

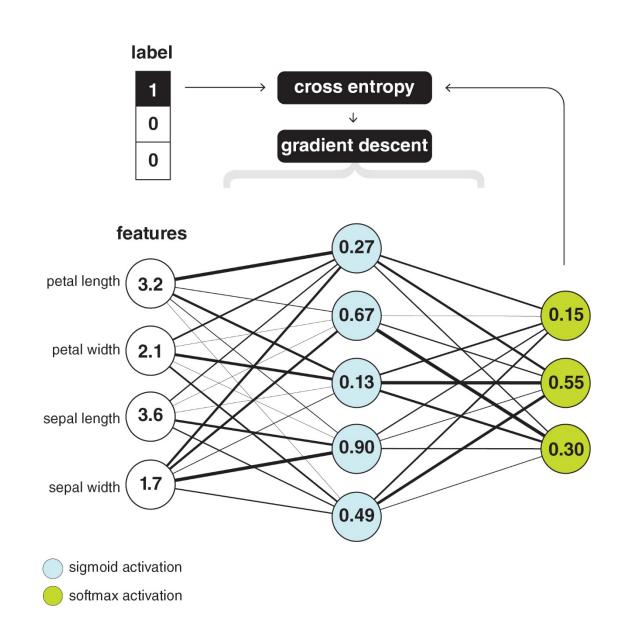
$$= - \eta \frac{\partial w}{\partial L}$$



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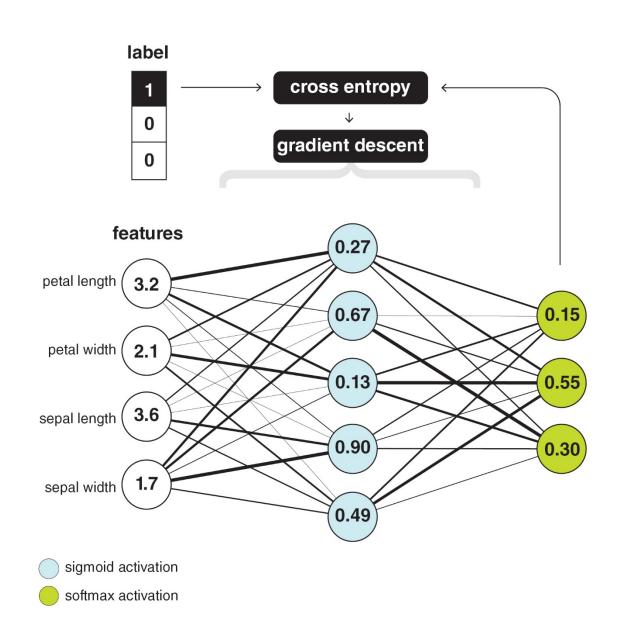
 $\Delta w \propto - \text{ gradient}$ $= -\frac{\partial L}{\partial w}$ $= -\eta \frac{\partial L}{\partial w}$



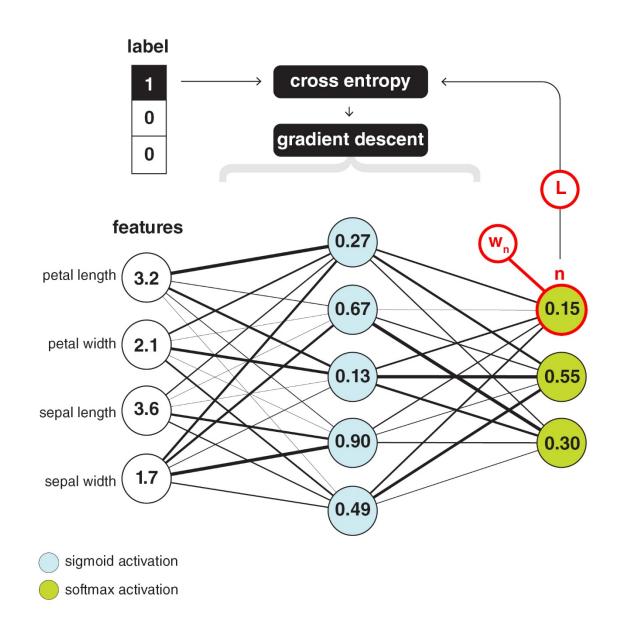


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f(f(input))

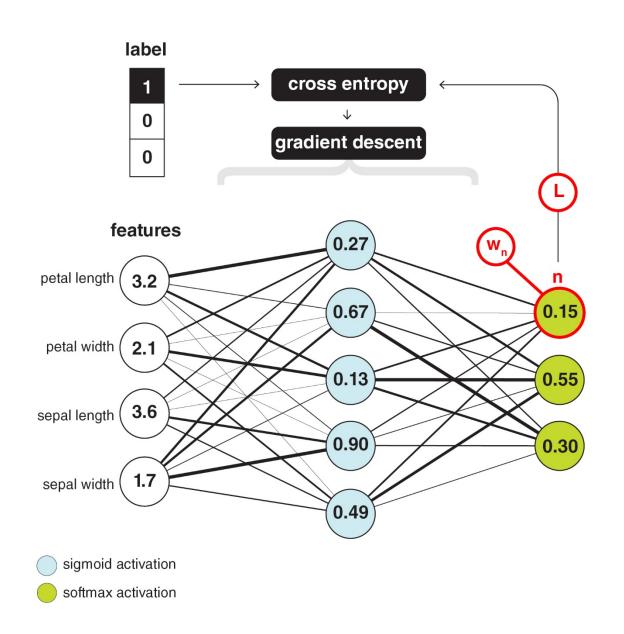


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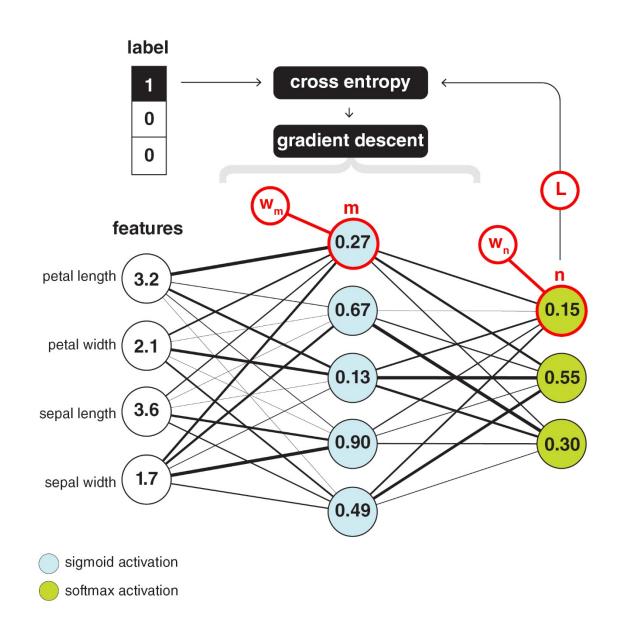


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- **5.** backpropagation + updates

$$\Delta w_{n} = -\eta \frac{\partial L}{\partial w_{n}}$$
$$= -\eta \frac{\partial L}{\partial so} \frac{\partial so}{\partial n} \frac{\partial n}{\partial w_{n}}$$



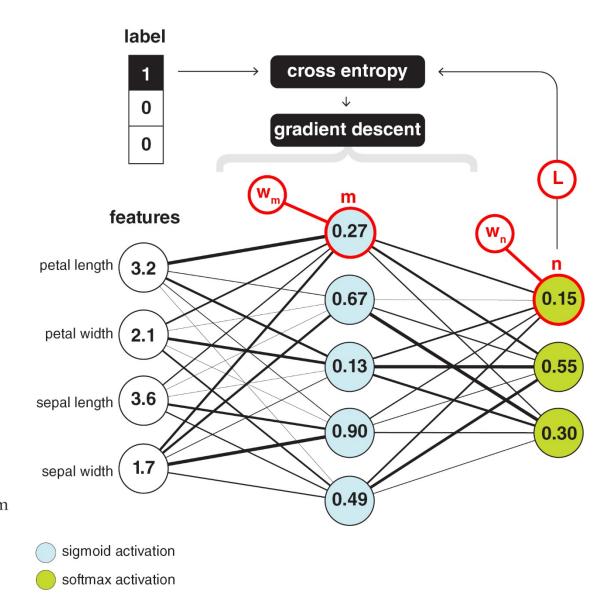
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- ✓ **Model:** 3-layer neural network
- ✓ Loss: cross entropy
- ✓ Optimizer: gradient descent
- 1. parameter initialization
- 2. data input
- **3.** forward propagation
- 4. loss calculation
- **5.** backpropagation + updates



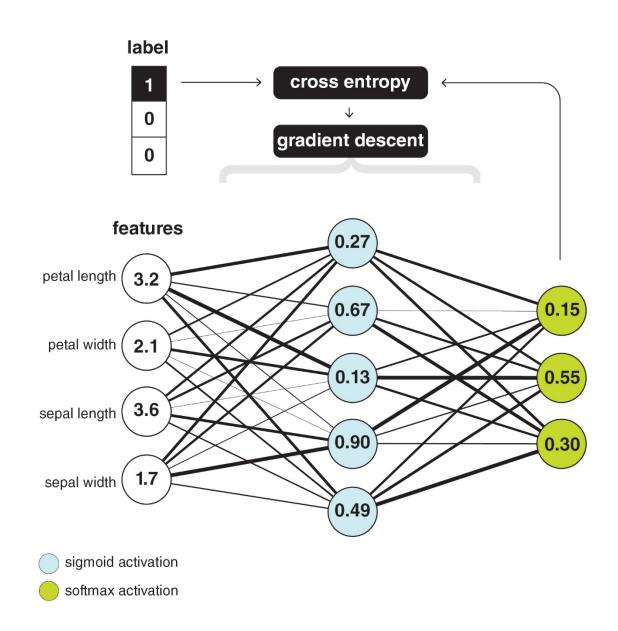
- ✓ Data: iris dataset
- ✓ Model: 3-layer neural network
- ✓ Loss: cross entropy
- ✓ Optimizer: gradient descent
- 1. parameter initialization
- 2. data input
- **3.** forward propagation
- 4. loss calculation
- **5.** backpropagation + updates

$$\Delta w_{m} = -\eta \frac{\partial L}{\partial w_{m}}$$

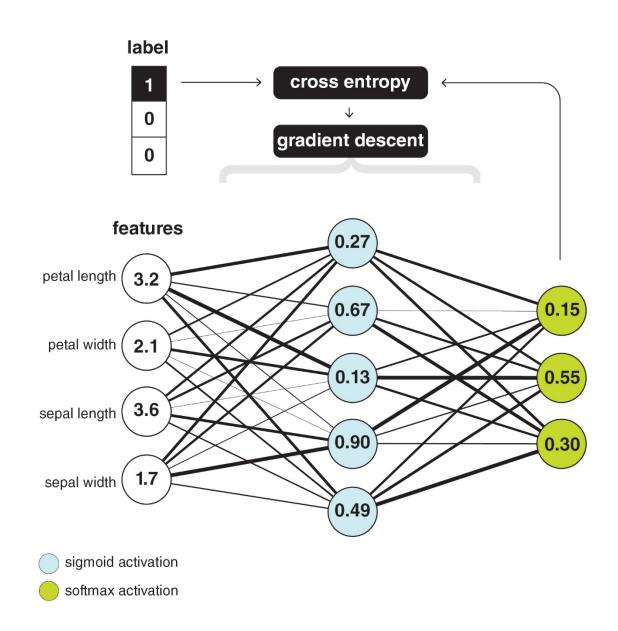
$$= -\eta \frac{\partial L}{\partial so} \frac{\partial so}{\partial n} \frac{\partial n}{\partial si} \frac{\partial si}{\partial m} \frac{\partial m}{\partial w_{m}}$$



- ✓ Data: iris dataset
- ✓ **Model:** 3-layer neural network
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- ✓ Data: iris dataset
- ✓ **Model:** 3-layer neural network
- ✓ Loss: cross entropy
- ✓ Optimizer: gradient descent
- 1. parameter initialization
- 2. data input
- **3.** forward propagation
- 4. loss calculation
- **5.** backpropagation + updates
- **6.** repeat 2,3,4, & 5



Gradient Descent Flavors

vanilla gradient descent - entire dataset stochastic gradient descent - random batch of samples (IID) online gradient descent - (need not be IID)

Gradient Descent Flavors

vanilla gradient descent - entire dataset
stochastic gradient descent - random batch of samples (IID)
online gradient descent - (need not be IID)

learning rate

batch size

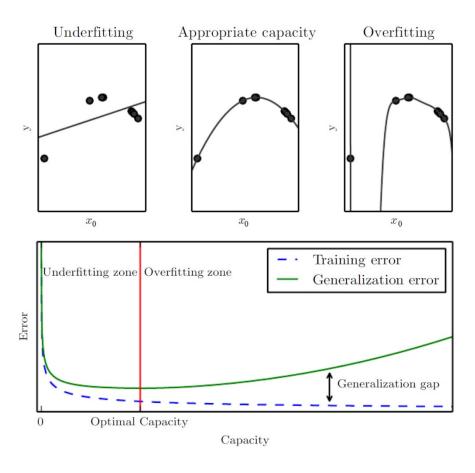
of epochs

What is the intuition behind neural networks?

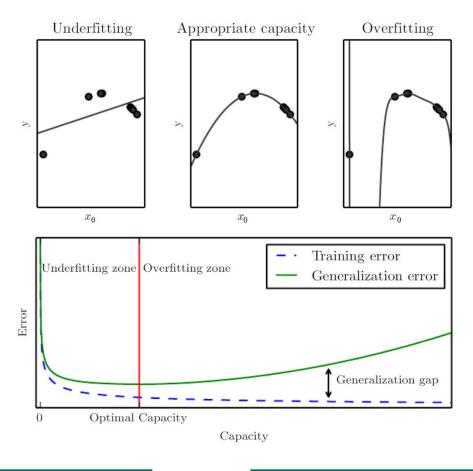
How do neural networks learn?

How to train neural networks?

The Perfect Fit



The Perfect Fit



parameters vs hyperparameters

Ian Goodfellow, Yoshua Bengio & Aaron Courville

Deep Learning MIT Press - 2016

Hyperparameters

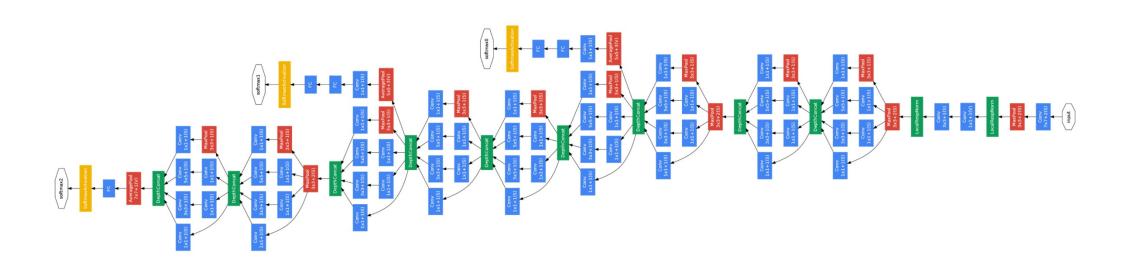
model-specific vs optimizer-specifc

architecture activations initializations loss functions optimizers regularizers

learning rate batch size # of epochs

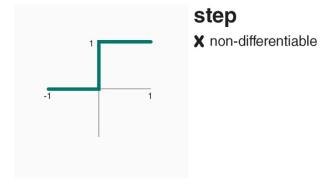
Architecture

of layers # of units/layer

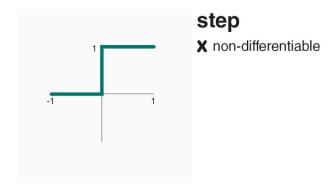


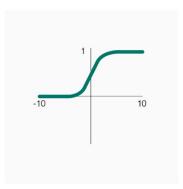
Christian Szegedy, Wei Liu, Yangqing Jia, et al.

Activations



Activations

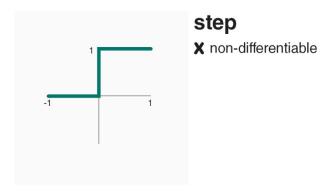


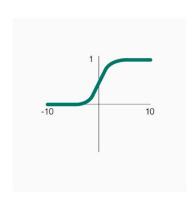


sigmoid

- ✓ smooth + step-like
 ✓ good activations close to 0
 ✓ activations are bound 0~1
 X vanishing gradients

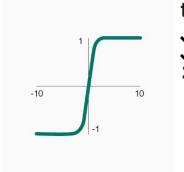
Activations





sigmoid

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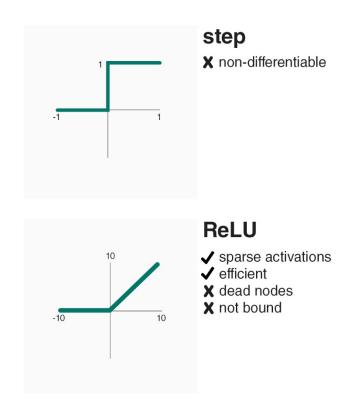


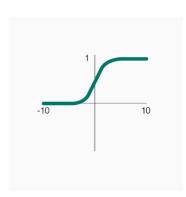
tanh

- ✓ scaled sigmoid
- ✓ stronger activations

 ★ vanishing gradients

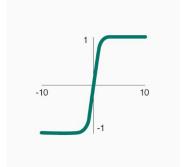
Yann LeCun, Leon Bottou, Genevieve B. Orr & Klaus -Robert Müller





sigmoid

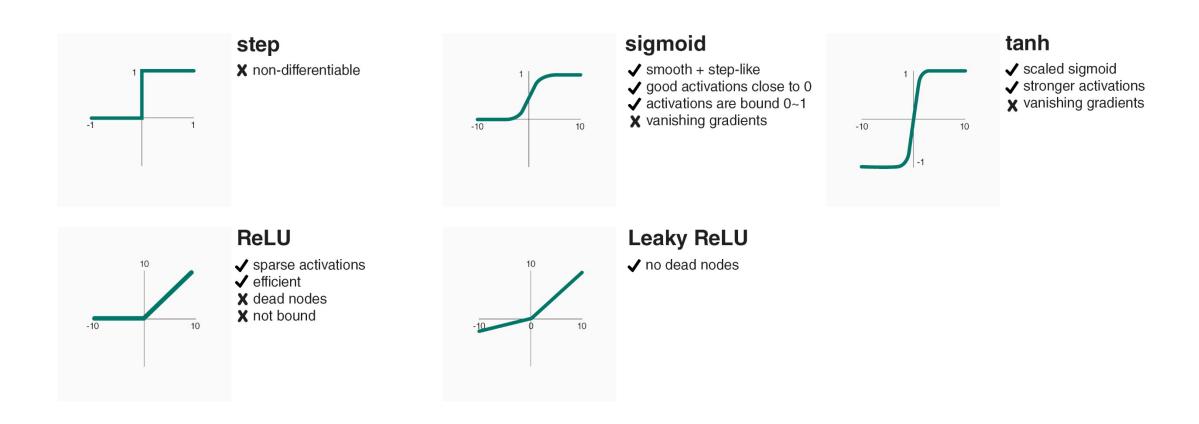
- ✓ smooth + step-like
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tanh

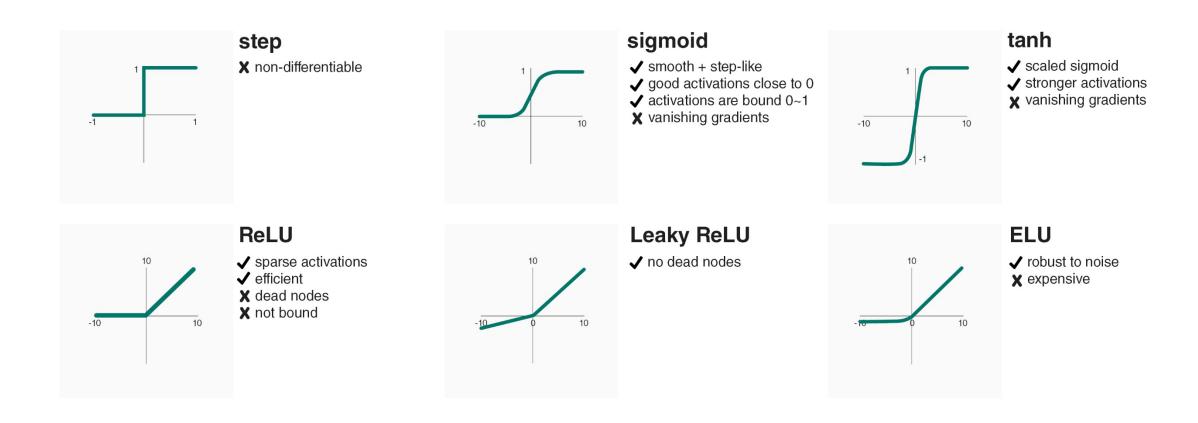
- ✓ scaled sigmoid
- ✓ stronger activations
- **x** vanishing gradients

Alex Krizhevsky, Ilya Sutskever & Geoffrey E. Hinton



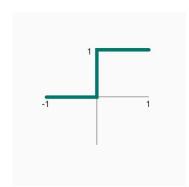
Kaiming He, Xiangyu Zhang, Shaoqing Ren & Jian Sun

Delving Deep into Rectifiers: Surpassing Human-Level Performance on ImageNet Classification International Conference on Computer Vision - ICCV 2015



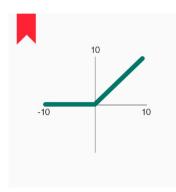
Djork-Arné Clevert, Thomas Unterthiner & Sepp Hochreiter

Fast and Accurate Deep Network Learning by Exponential Linear Units (ELUs)
International Conference on Computer Vision - ICCV 2015



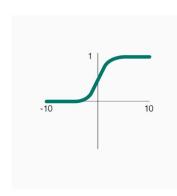
step

X non-differentiable



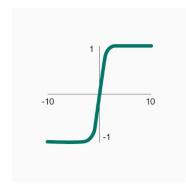
ReLU

- ✓ sparse activations
- ✓ efficient
- X dead nodes
- X not bound



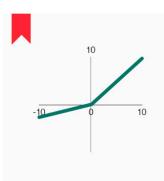
sigmoid

- ✓ smooth + step-like
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- **X** vanishing gradients



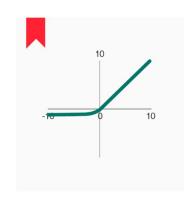
tanh

- ✓ scaled sigmoid
- ✓ stronger activations ★ vanishing gradients



Leaky ReLU

✓ no dead nodes

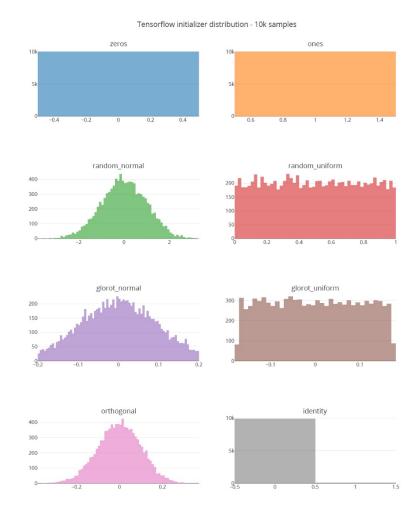


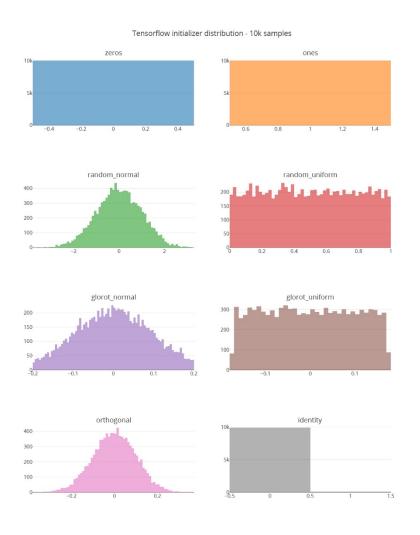
ELU

- ✓ robust to noise
- **x** expensive

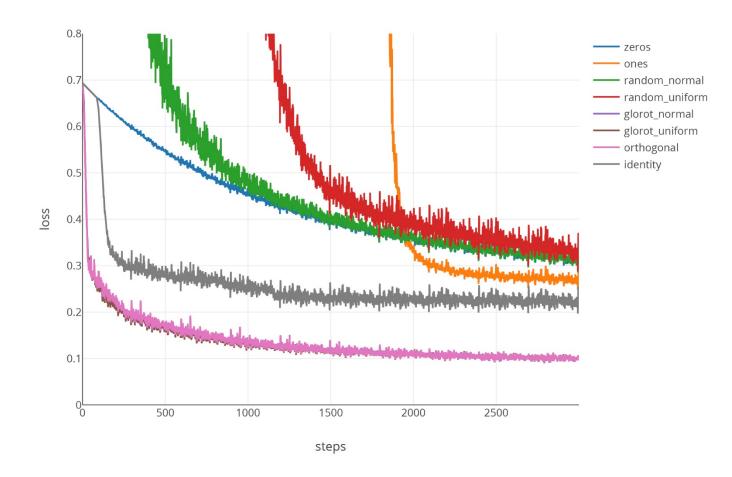
0 - stuck at a saddle point
 constants - difficult to break the symmetry
 large random values - small gradients, slow convergence







Step loss with different weight initialization



	Name	α	β	γ	Reference
	Constant	$\alpha = 0$	$\beta = 0$	$\gamma \ge 0$	used by [ZF14]
\rightarrow	Xavier/Glorot uniform	$\alpha = \sqrt{\frac{6}{n_{in} + n_{out}}}$	$\beta = 0$,	[GB10]
\rightarrow	Xavier/Glorot normal	$\alpha = 0$	$\beta = \left(\frac{2}{(n_{in} + n_{out})}\right)^2$	$\gamma = 0$	[GB10]
\rightarrow	Не	$\alpha = 0$	$eta=rac{2}{n_{in}}$	$\gamma = 0$	[HZRS15b]
	Orthogonal	_	_	$\gamma = 0$	[SMG13]
	LSUV	_	_	$\gamma = 0$	[MM15]

Table B.2.: Weight initialization schemes of the form $w \sim \alpha \cdot \mathcal{U}[-1,1] + \beta \cdot \mathcal{N}(0,1) + \gamma$.

 n_{in} , n_{out} are the number of units in the previous layer and the next layer. Typically, biases are initialized with constant 0 and weights by one of the other schemes to prevent unit-coadaptation. However, dropout makes it possible to use constant initialization for all parameters.

LSUV and Orthogonal initialization cannot be described with this simple pattern.

Loss Functions

regression - mean squared error

multiclass classification - categorical cross entropy

pixel classification - dice/ Wasserstein dice coefficient

stochastic gradient descent + momentum

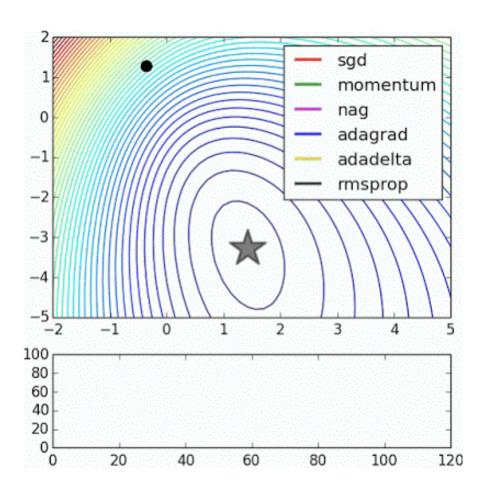
stochastic gradient descent + momentum

adaptive gradient (AdaGrad)

stochastic gradient descent + momentum

adaptive gradient (AdaGrad)

root mean square propagation (RMSProp)



L1, L2 regularization

$$\mathcal{L}_{new} = \mathcal{L} + \frac{\lambda}{2}|W|$$

$$\mathcal{L}_{new} = \mathcal{L} + \frac{\lambda}{2} W^2$$

L1, L2 regularization

$$\mathcal{L}_{new} = \mathcal{L} + \frac{\lambda}{2}|W|$$

$$\mathcal{L}_{new} = \mathcal{L} + \frac{\lambda}{2} W^2$$



dropout

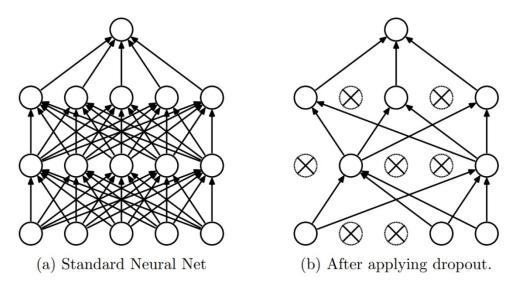
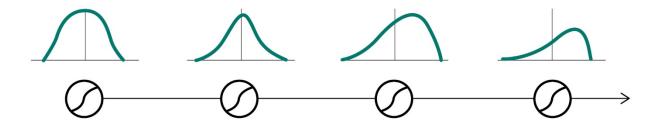


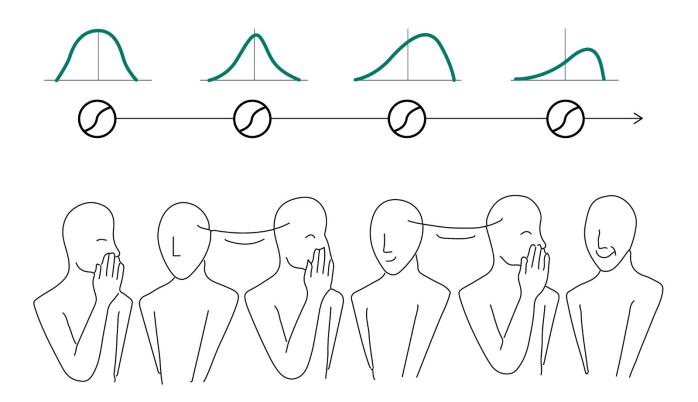
Figure 1: Dropout Neural Net Model. **Left**: A standard neural net with 2 hidden layers. **Right**: An example of a thinned net produced by applying dropout to the network on the left. Crossed units have been dropped.

Nitish Srivastava, Geoffrey Hinton, Alex Krizhevsky, Ilya Sutskever & Ruslan Salakhutdinov

batch normalization



batch normalization

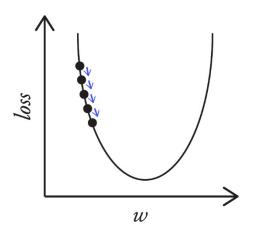


Sergey Ioffe & Christian Szegedy

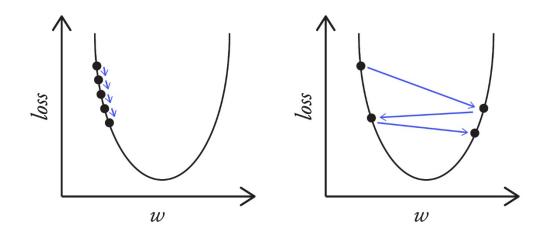
Batch Normalization: Accelerating Deep Network Training by Reducing Internal Covariate Shift Journal of Machine Learning Research - 2014

learning rate

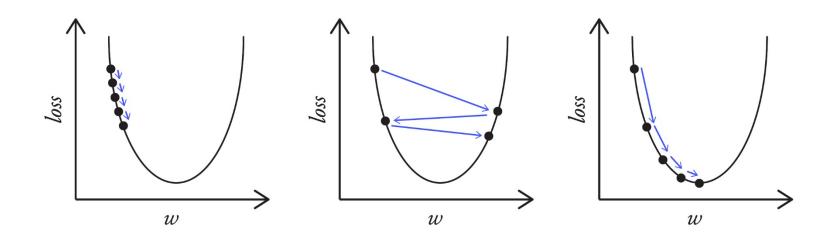
learning rate



learning rate

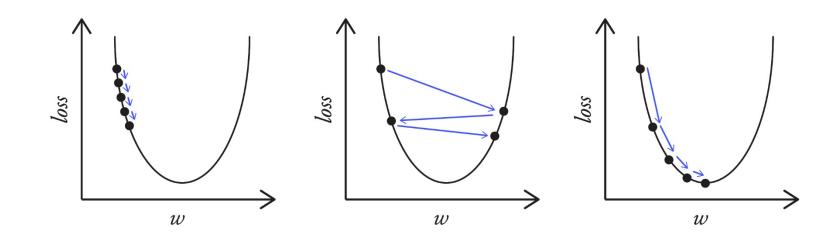


learning rate



learning rate

0.1, 0.01, 0.001, 0.0001,...

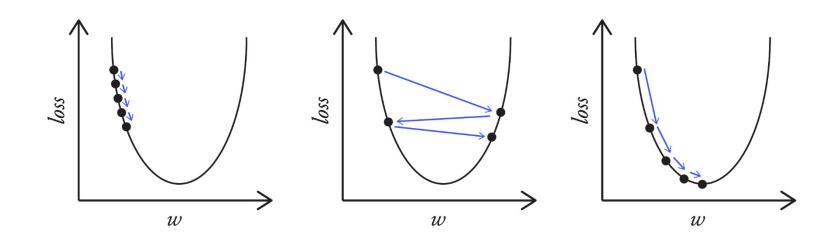


batch size

16, 32, 64, 128,...

learning rate

0.1, 0.01, 0.001, 0.0001,...

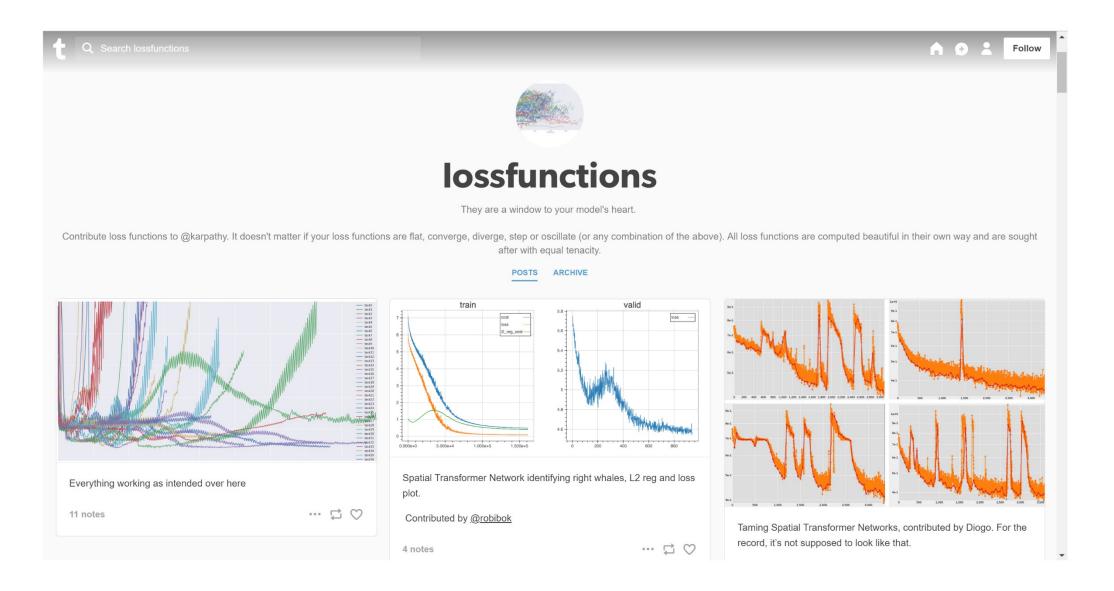


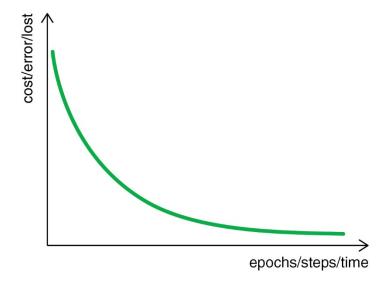
batch size

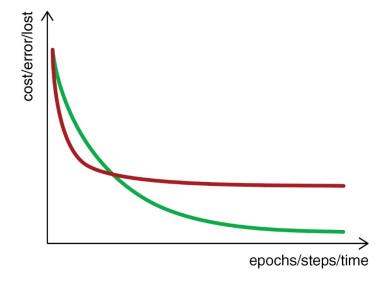
16, 32, 64, 128,...

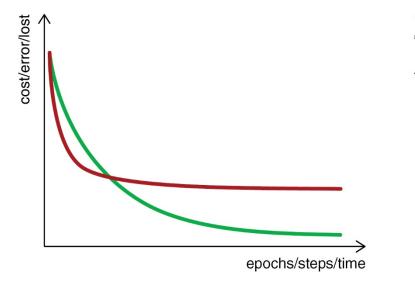
of epochs early stopping

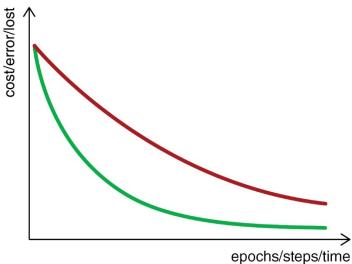
Babysitting your Network

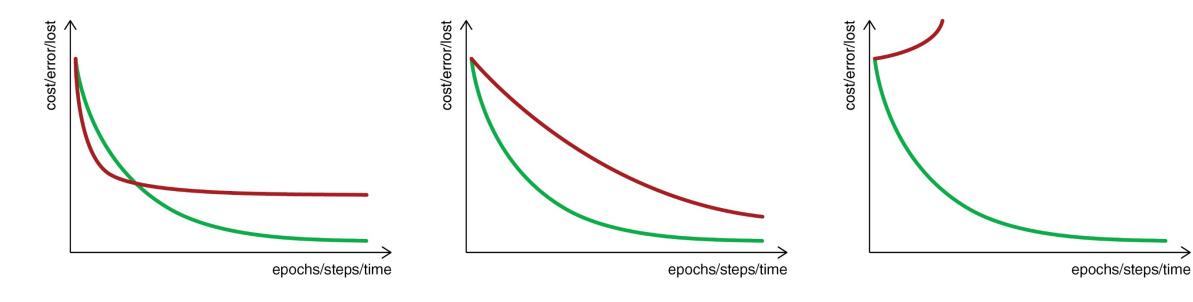


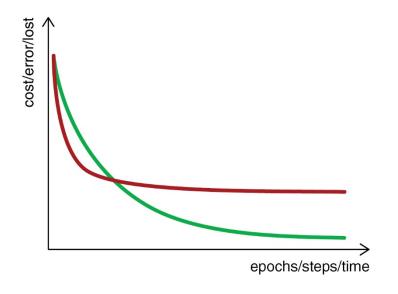


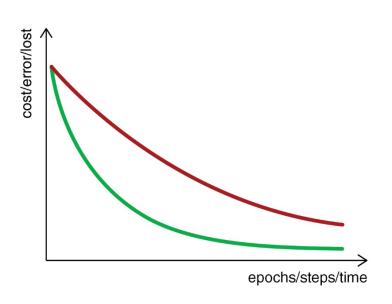


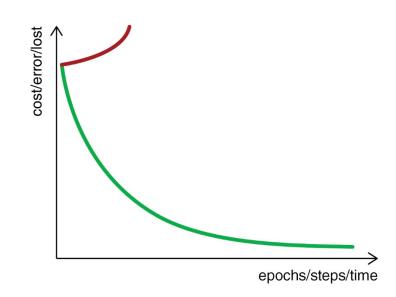


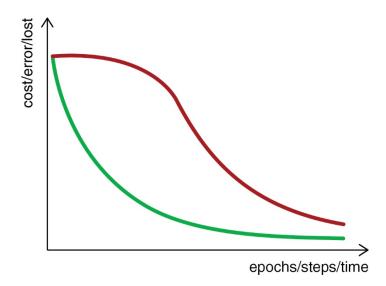


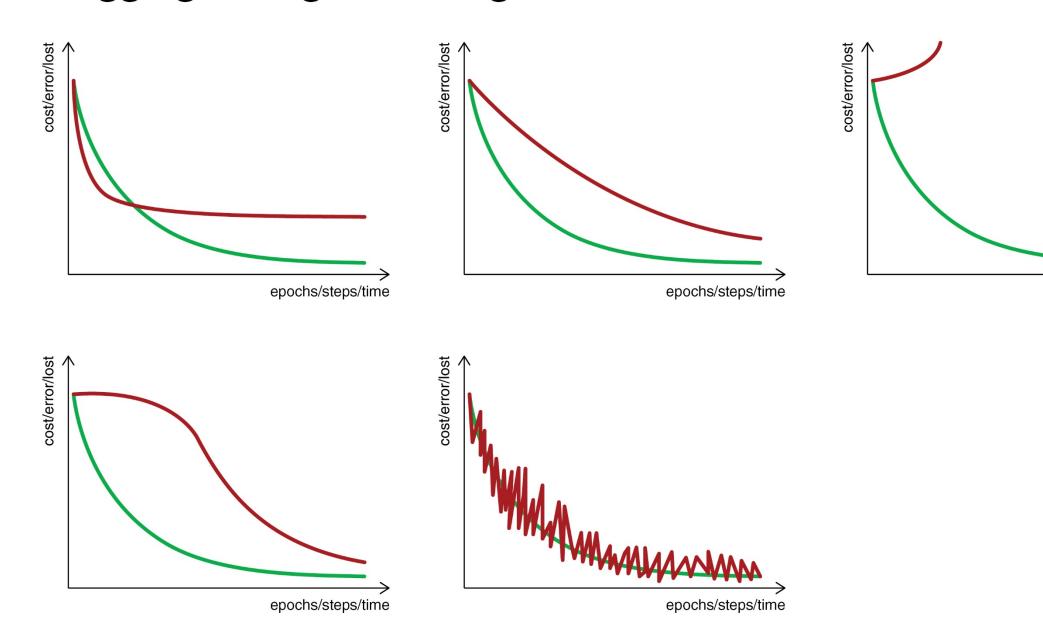












epochs/steps/time

